

Computational Structural Mechanics and Dynamics

Assignment 9 – Nicolas Andre Caronte Grønland

Tasks:

- Describe in extension how can be applied a non symmetric load on this formulation.
- Using thin beams formulation, describe the shape of the B(e) matrix and comment the integration rule.

Problem a)

We are now considering an axisymmetrical shell with non symmetric loading. For a non-axisymmetric load we have to reconsider the right hand side of the system of equations. To do this one has to express the displacements and force components through Fourier-series, and after that one can solve the problem numerically.

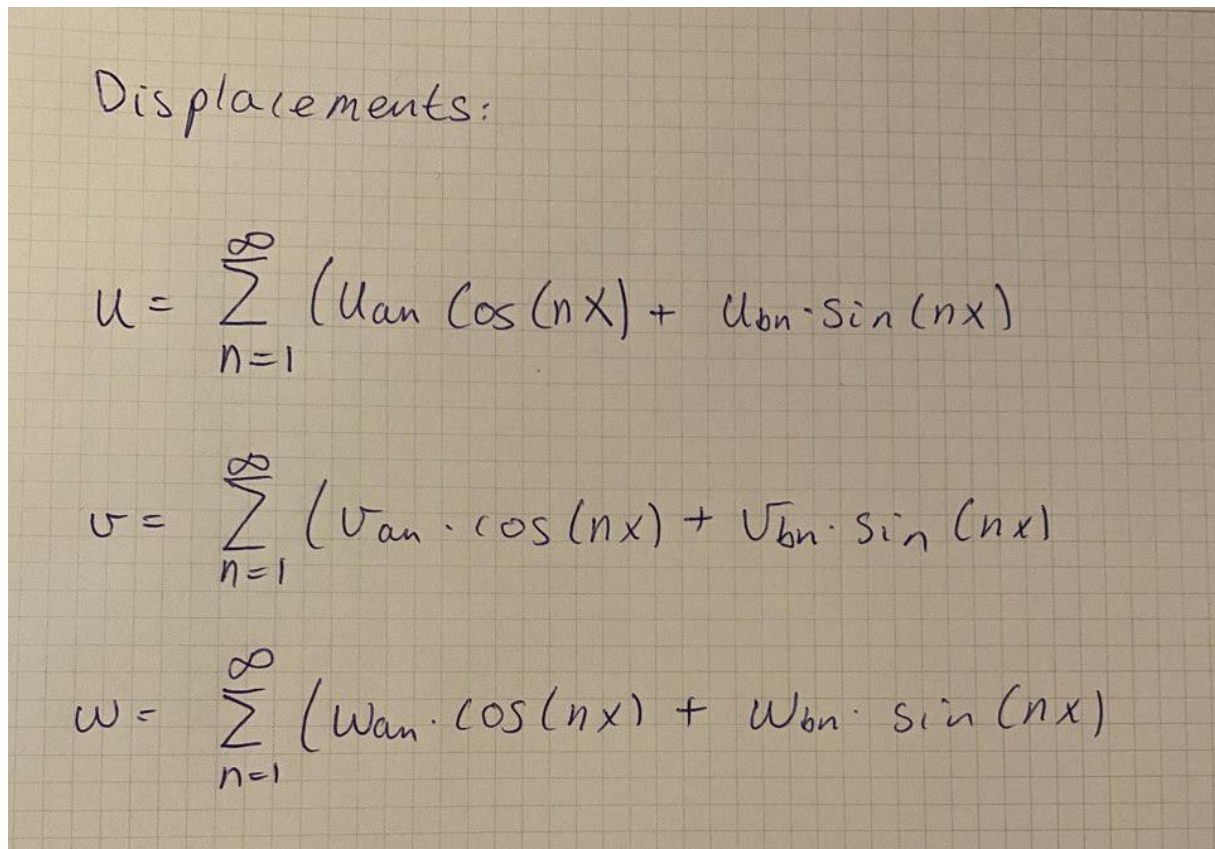
Expressing the force components, right hand side:

Force:

$$f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos(nx) + b_n \sin(nx))$$
$$a_0 = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) dx$$
$$a_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cos(nx) dx$$
$$b_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \sin(nx) dx$$

Note that x represents the circumferential direction.

Expressing the displacements:



Displacements:

$$u = \sum_{n=1}^{\infty} (U_{an} \cos(nx) + U_{bn} \sin(nx))$$
$$v = \sum_{n=1}^{\infty} (V_{an} \cdot \cos(nx) + V_{bn} \cdot \sin(nx))$$
$$w = \sum_{n=1}^{\infty} (W_{an} \cdot \cos(nx) + W_{bn} \cdot \sin(nx))$$

u, v and w are the axial, radial and circumferential displacements respectively.

Problem b)

The shear effects arise, but are neglected for thin beam formulation. This means that the $B(e)$ matrix will consist of the bending part, B_b , and the membrane part, B_m . For the membrane part, membrane locking will arise for fully integrated elements, thus giving a stiffer solution. As for handling shear locking one can handle membrane locking by reduced integration of the membrane part of the K-matrix.